

Linear adversarial training, robustness in machine learning and applications to cardiology

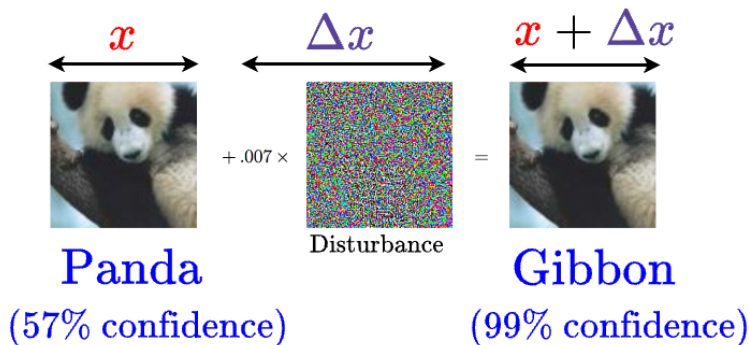
Antônio H. Ribeiro

Uppsala University, Sweden

KTH, Royal Institute of Technology
Stockholm, Sweden

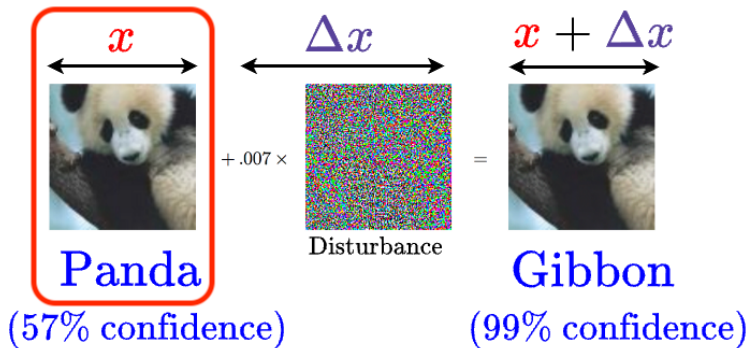
2023

Adversarial attacks



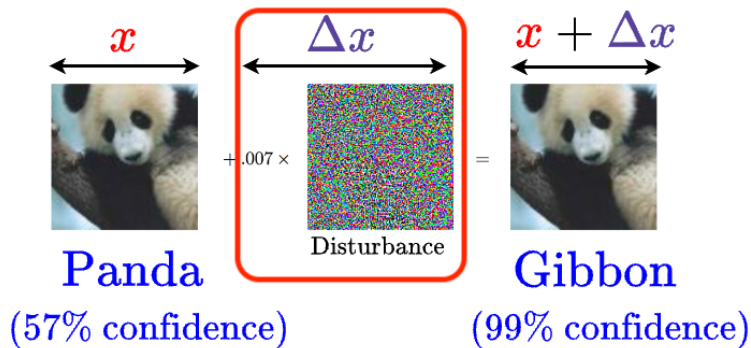
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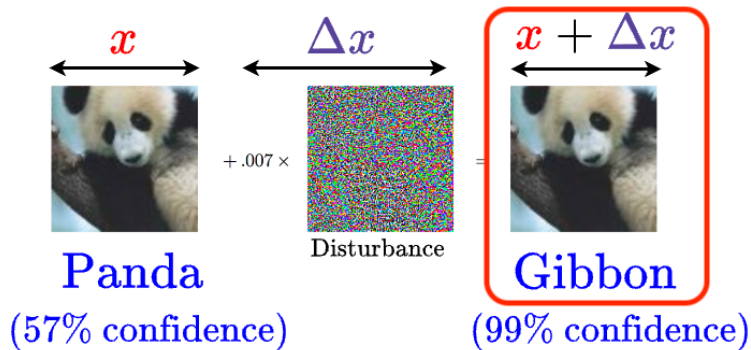
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I. J. Goodfellow, J. Shlens, C. Szegedy. Explaining and Harnessing Adversarial Examples, ICLR (2015)

Adversarial training: *Each training sample is modified by an adversary.*

Part I. Linear adversarial training

Regularization properties of adversarially-trained linear regression

Antônio H. Ribeiro, Dave Zachariah, Francis Bach, Thomas B. Schön.

NeurIPS (2023) - **Spotlight**

Part II. Robustness of overparameterized models

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Adversarially-trained linear regression

► **Linear regression:**

$$\min_{\beta} \sum_{i=1}^{\#train} (y_i - \beta^\top x_i)^2$$

Adversarially-trained linear regression

► Linear regression:

$$\min_{\beta} \sum_{i=1}^{\#train} (\underbrace{y_i}_{\text{observed}} - \underbrace{\beta^T x_i}_{\text{linear prediction}})^2$$

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$$(y_i - \beta^{\top} (x_i + \Delta x_i))^2$$

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$$\sum_{i=1}^{\#train} \max_{\|\Delta x_i\| \leq \delta} (y_i - (x_i + \Delta x_i)^T \beta)^2$$

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$$\sum_{i=1}^{\#train} \max_{\|\Delta x_i\| \leq \delta} (y_i - (x_i + \Delta x_i)^T \beta)^2$$

It can be rewritten as:

$$\sum_{i=1}^{\#train} \left(|y_i - x_i^T \beta| + \delta \|\beta\|_* \right)^2$$

where $\|\cdot\|_*$ is the dual norm.

Adversarially-trained linear regression

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Similarities with Lasso

► ℓ_∞ -adversarial attacks:

$$\sum_{i=1}^{\#train} \left(|y_i - \mathbf{x}_i^T \boldsymbol{\beta}| + \delta \|\boldsymbol{\beta}\|_1 \right)^2$$

► Lasso:

$$\sum_{i=1}^{\#train} \left(|y_i - \mathbf{x}_i^T \boldsymbol{\beta}| \right)^2 + \lambda \|\boldsymbol{\beta}\|_1.$$

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Main results:

#1. **Map** $\lambda \leftrightarrow \delta$ for which they yield the **same result**.

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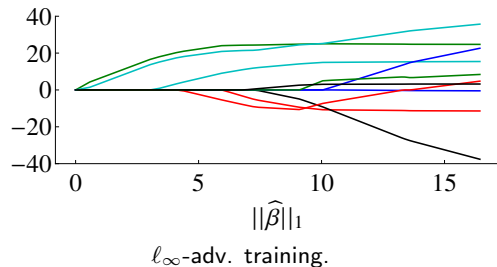
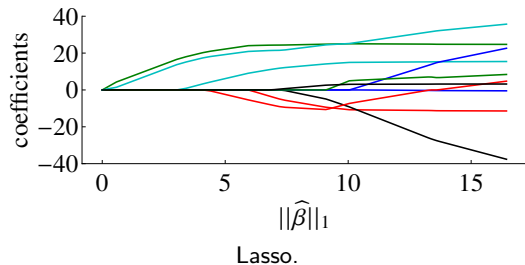
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Main results:

- #1. **Map** $\lambda \leftrightarrow \delta$ for which they yield the **same result**.
- #2. **More parameters than data**: abrupt transition into interpolation.
- #3. **Optimal choice** of δ independent on noise level.

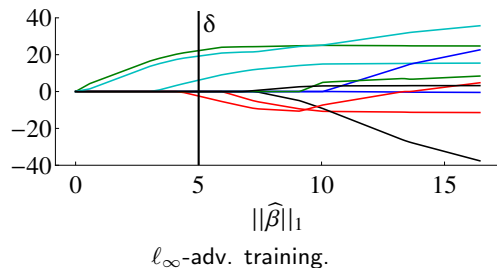
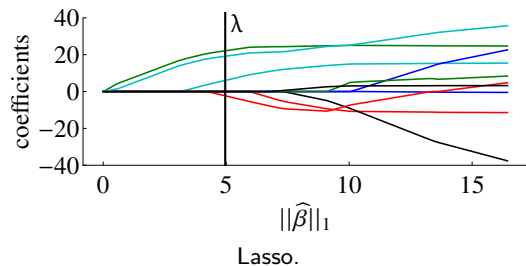
1. Equivalence with Lasso

Map $\lambda \leftrightarrow \delta$ for which they yield the **same result**.



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The that yield the **same result** are **not** necessarily the same, i.e.: $\delta \neq \lambda$

2. More parameters than data

Lasso: transition **only in the limit**

$$\lambda \rightarrow 0^+ \Rightarrow \sum_{i=1}^{\#train} \left(y_i - \mathbf{x}_i^T \boldsymbol{\beta} \right)^2 \rightarrow 0$$

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Adversarial training:

$$\delta \in (0, \text{threshold}] \Rightarrow \sum_{i=1}^{\#train} \left(y_i - \mathbf{x}_i^T \boldsymbol{\beta} \right)^2 = 0$$

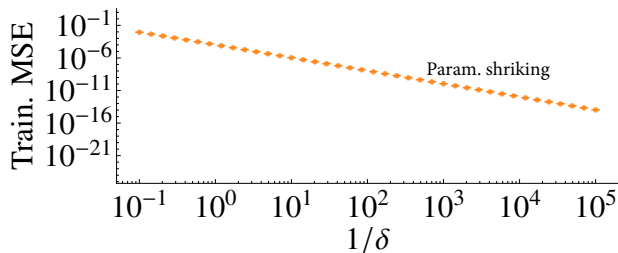
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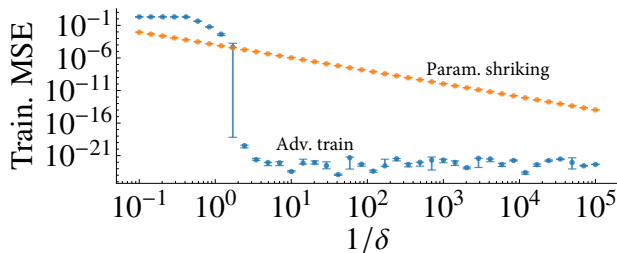
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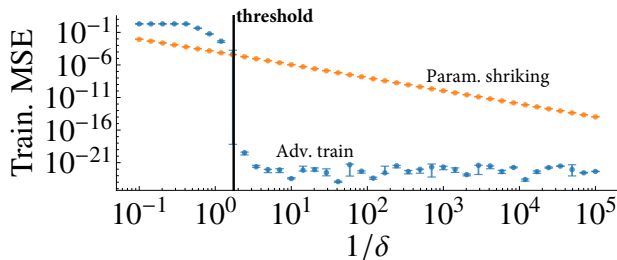
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2. Equivalence with minimum norm interpolator

For $\delta \in (0, \text{threshold}]$, the minimum-norm interpolator is the solution to adversarial training.

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Relevance

Connect **adversarial training** with **double descent** and **benign overfitting**

3. Invariance to noise levels

To obtain near-oracle performance.

► *Lasso:*

$$\lambda \propto \sigma \sqrt{\log(\#params)/\#train}$$

► *ℓ_∞ -adversarial attack:*

$$\delta \propto \sqrt{\log(\#params)/\#train}$$

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Data model

$$y = \underbrace{x^\top \beta^*}_{\text{signal}} + \underbrace{\sigma}_{\text{noise std.}} \varepsilon.$$

Regularization properties of adversarially-trained linear regression

Additional results:

- ▶ ℓ_2 -adv. attacks and ridge regression.

Regularization properties of adversarially-trained linear regression

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NeurIPS (2023) - **Spotlight**

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- ▶ Generalization to **other loss** functions
- ▶ Connection to **robust regression** and $\sqrt{\text{Lasso}}$.

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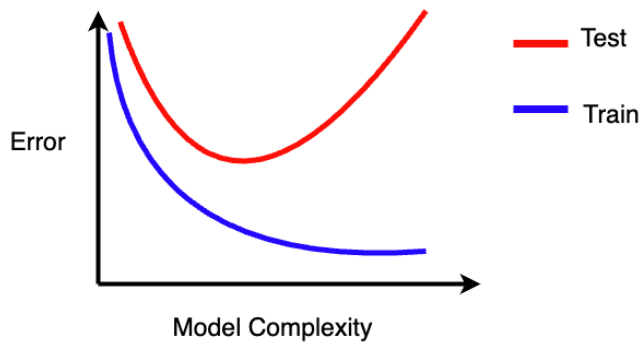
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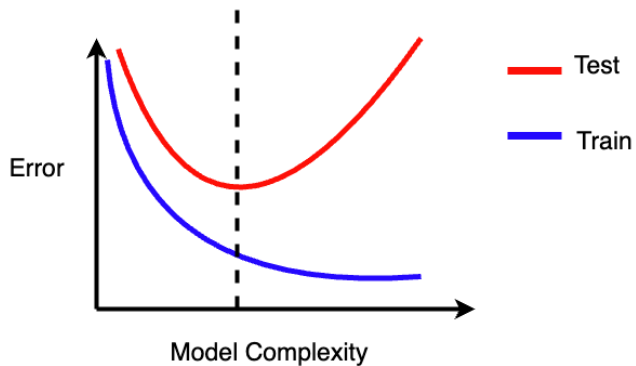
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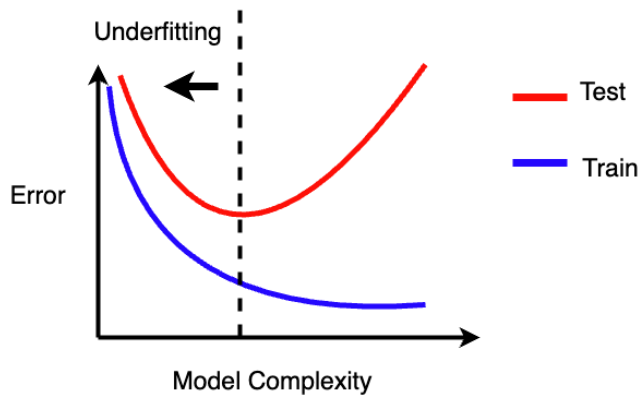
Generalization to new test points



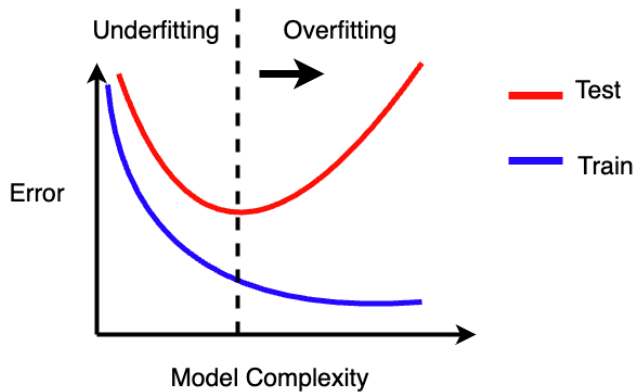
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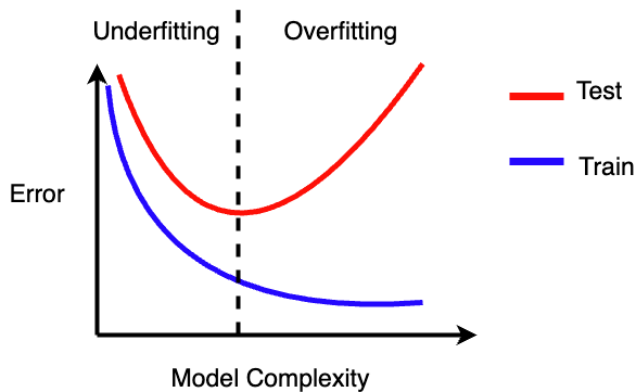
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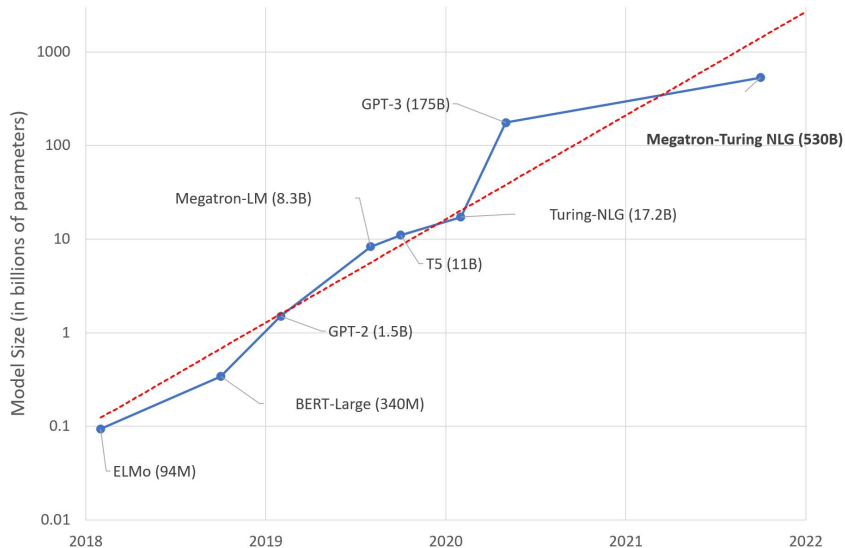
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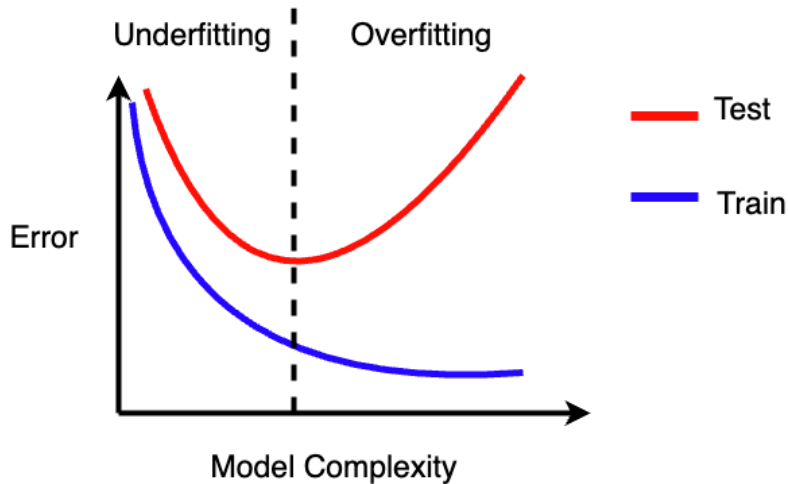


Generalization of deep neural networks



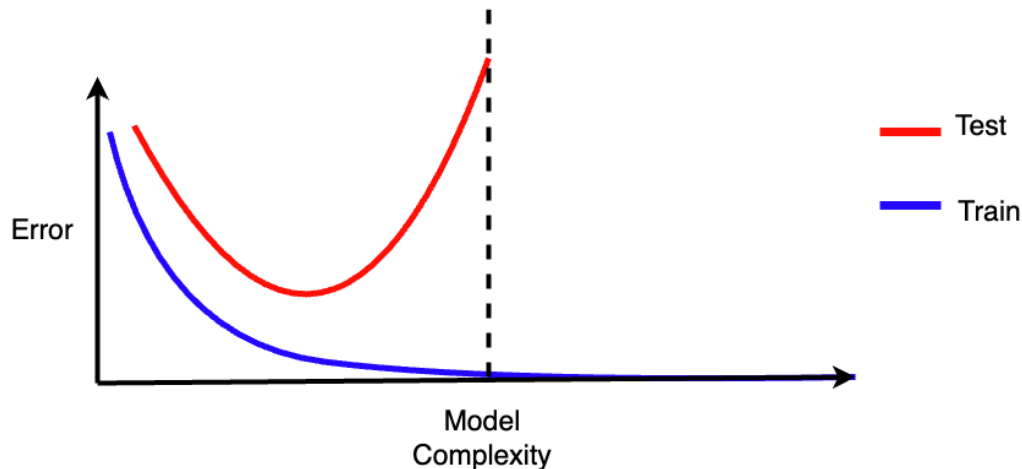
C. Zhang, S. Bengio, M. Hardt, B. Recht, and O. Vinyals. Understanding deep learning requires rethinking generalization. ICLR, 2017

Double-descent curves



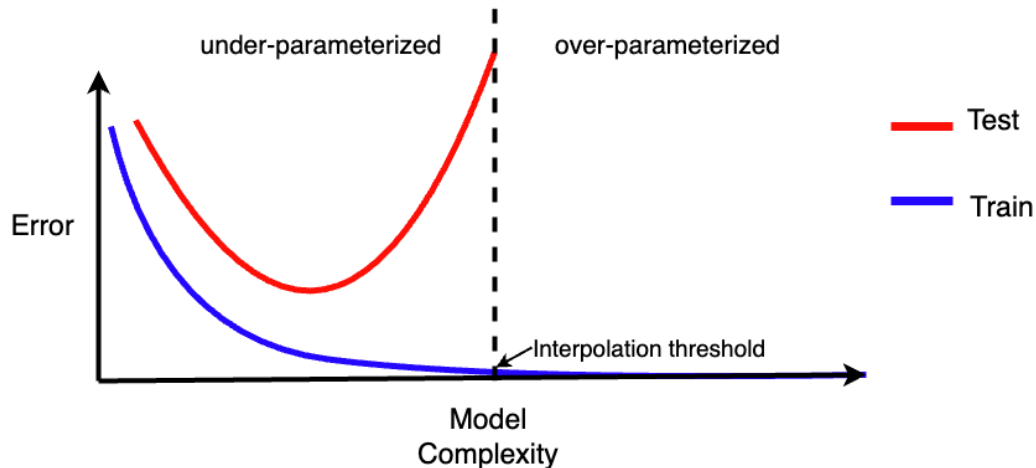
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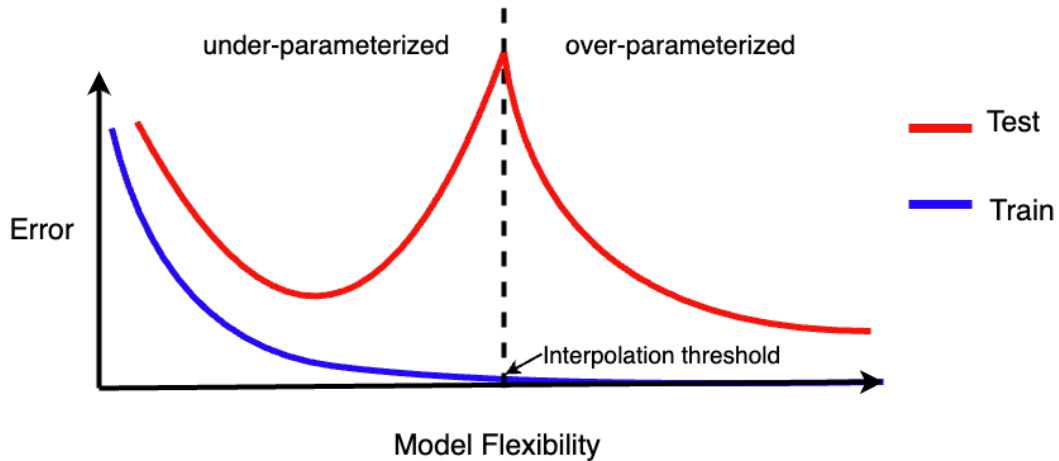
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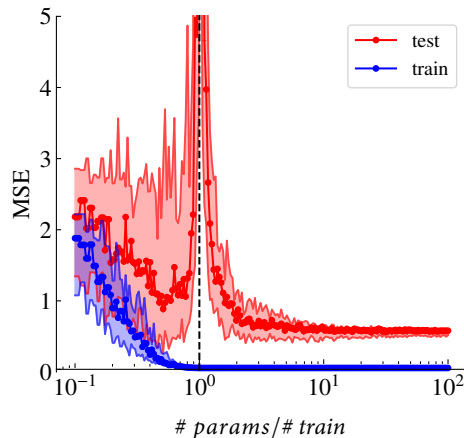
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Double-descent

- ▶ Ph.D. seminar **course**:
*The unreasonable effectiveness of
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Double-descent

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Beyond Occam's Razor in System Identification: Double-Descent when Modeling Dynamics

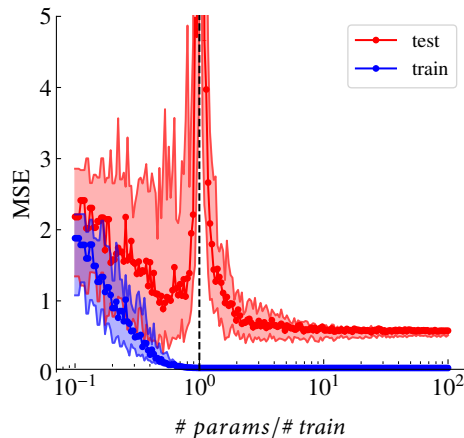
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Honorable mention: **Young author award**

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Deep networks for system identification: a Survey

Gianluigi Pillonetto, Aleksandr Aravkin, Daniel Gedon, Lennart Ljung, Antonio H. Ribeiro, Thomas Bo Schön.

Automatica (Provisionally accepted), 2023.

Can **double descent** be observed **in adversarial settings**?

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Given a **test point** (\mathbf{x}_0, y_0) , the error is:

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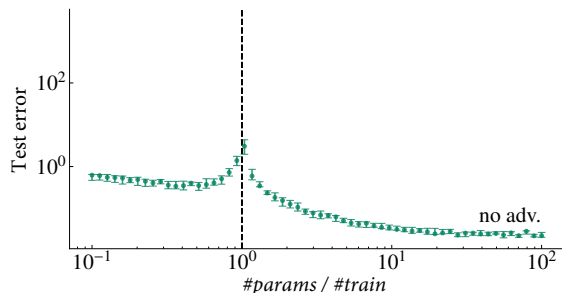


Figure: Adv. risk. min. ℓ_2 -norm interpolator

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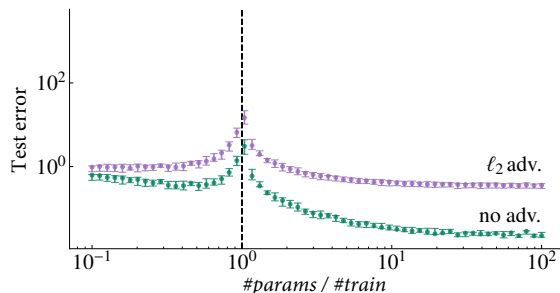


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- ▶ ℓ_∞ -adversary

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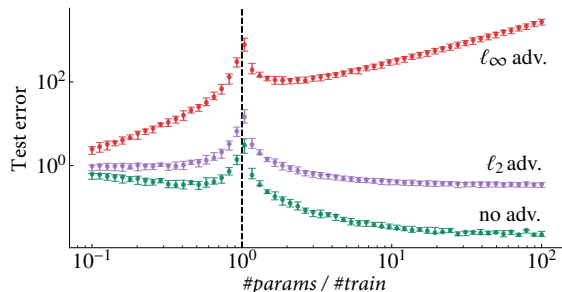


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Interpretation

Minimum ℓ_2 -norm interpolation \Leftrightarrow ℓ_2 -adversarial training. (Result #2, Part I)

Overparameterized Linear Regression under Adversarial Attack

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Analysis:

- ▶ **Asymptotic results** showing the phenomena
- ▶ **Non-asymptotic results**: concentration inequalities

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The electrocardiogram (ECG) exam

Cardiovascular diseases:

- ▶ \approx 18 million **deaths** in 2019 (**32%**).

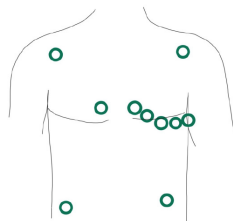
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The ECG is the **major diagnostic tool**.

- ▶ Low-cost, safe and non-invasive
- ▶ Can detect arrhythmias, myocardial infarction, cardiomyopathy...



Left: ECG signal **Right:** Electrode placement.

Computational electrocardiography



Figure Automated ECG interpretation Glasgow (1971).

Macfarlane, P.W.; Kennedy, J. "Automated ECG Interpretation—A Brief History from High Expectations to Deepest Networks." *Hearts* 2021.

The transition into end-to-end learning

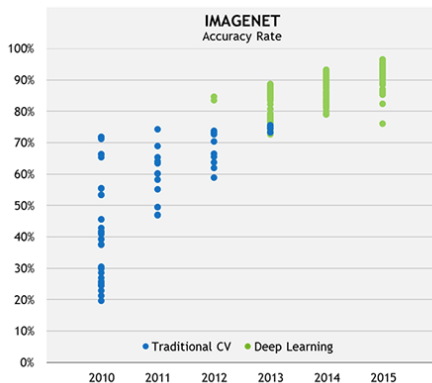


Figure: Accuracy on Imagenet as models transitioned from feature extraction to end-to-end.

J. Deng, W. Dong, R. Socher, L.-J. Li, K. Li, and L. Fei-Fei, "Imagenet: A large-scale hierarchical image database," CVPR (2009)

Telehealth and automatic diagnosis



Figure: State of Minas Gerais

Telehealth and automatic diagnosis

Telehealth Center of Minas Gerais

- ▶ 1100 municipalities
- ▶ > 3 500 ECGs per day

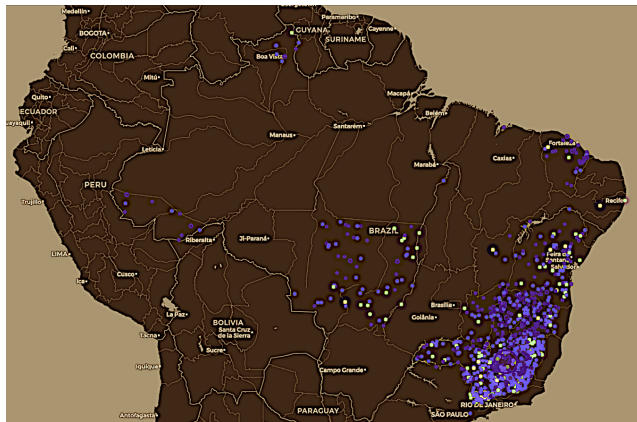


Figure: Municipalities assisted by the telehealth center

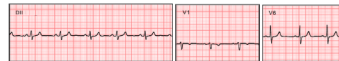
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- ▶ CODE dataset: historical data 2010 to 2017.
 - ▶ $n = 1.6\text{M}$ patients

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No abnormalities



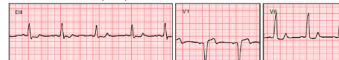
1st degree AV block (1dAVb)



Right bundle branch block (RBBB)



Left bundle branch block (LBBB)



Sinus bradycardia (SB)



Atrial fibrillation (AF)

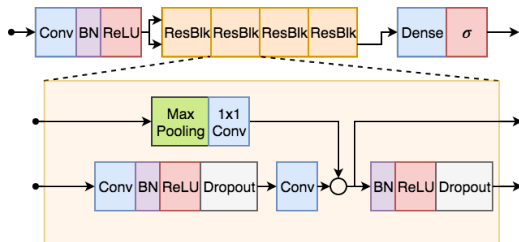


Sinus tachycardia (ST)



Automatic diagnosis of the ECG

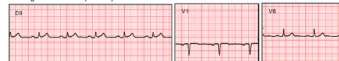
- ▶ CODE dataset: historical data 2010 to 2017.
 - ▶ $n = 1.6\text{M}$ patients
- ▶ Develop and evaluate deep neural network



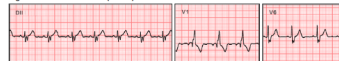
No abnormalities



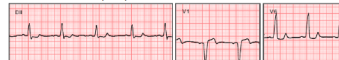
1st degree AV block (1dAVb)



Right bundle branch block (RBBB)



Left bundle branch block (LBBB)



Sinus bradycardia (SB)



Atrial fibrillation (AF)

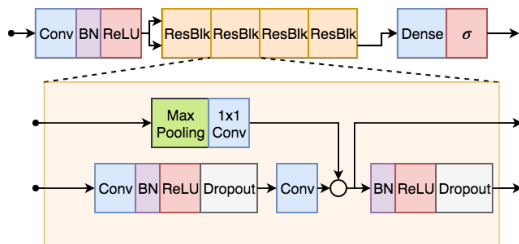


Sinus tachycardia (ST)



Automatic diagnosis of the ECG

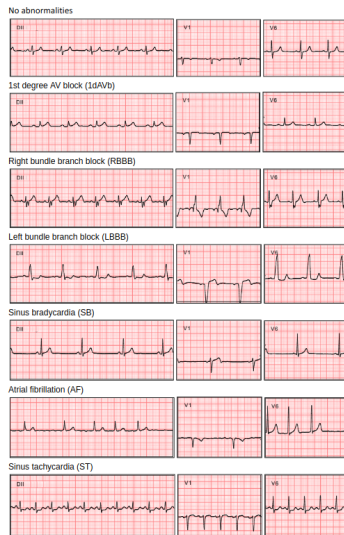
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Automatic diagnosis of the 12-lead ECG using a deep neural network

A. H. Ribeiro, M.H. Ribeiro, Paixão, G.M.M. et al

Nature Communications (2020)



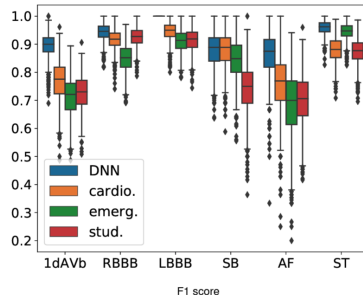
Automatic diagnosis of the ECG (cont.)

- **Result:** Deep neural network (DNN) performs at least as well as experts

cardio. → 4th year cardiology residents

emerg. → 3rd year emergency residents

stud. → 5th year Medical students



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Automatic diagnosis of the ECG (cont.)

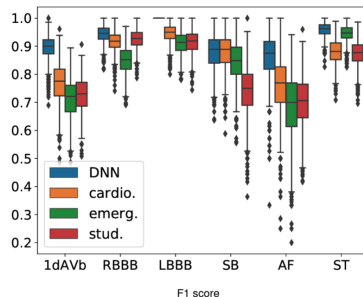
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- **Goal:** Improve the **accuracy**



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Automatic diagnosis of the ECG (cont.)

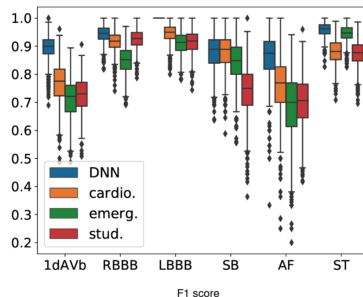
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- **Goal:** Improve the **accuracy**
assist **more patients**



Automatic diagnosis of the 12-lead ECG using a deep neural network

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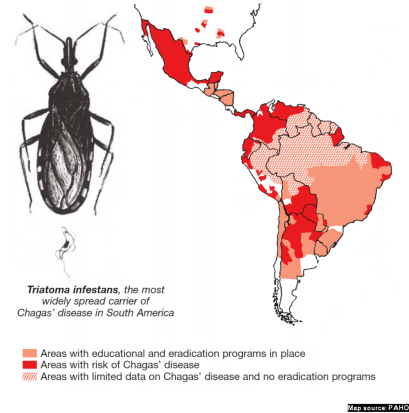
Nature Communications (2020)

Three directions

1. Automatic diagnosis;
2. Screening;
3. Prognosis.

Screening for Chagas disease from the ECG using deep neural networks

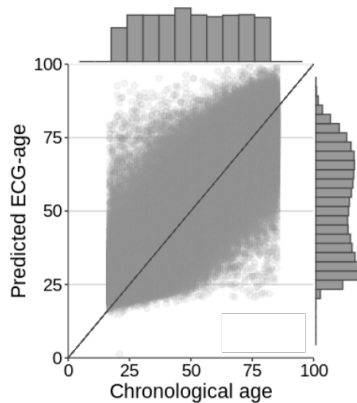
- ▶ **6 million** people infected.
- ▶ Diagnosed with **blood test**.
- ▶ Early diagnosis and treatment **halt progression**.
- ▶ **Low detection rates**



Screening for Chagas disease from the electrocardiogram using a deep neural network

Carl Jidling, Daniel Gedon, Thomas B. Schön, Claudia Di Lorenzo Oliveira, Clareci Silva Cardoso, Ariela Mota Ferreira, Luana Giatti, Sandhi Maria Barreto, Ester C. Sabino, Antônio L. P. Ribeiro, **Antônio H. Ribeiro**
Plos Neglected Tropical Diseases (2023)

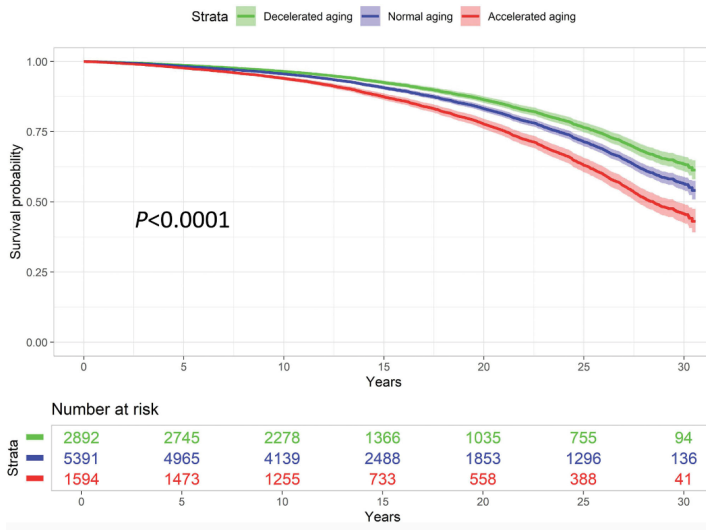
ECG predicted-age



Deep neural network estimated electrocardiographic-age as a mortality predictor

Emilly M. Lima*, Antônio H. Ribeiro*, Gabriela MM Paixão*, et. al. *Equal contribution*
Nature Communications (2021)

Risk predictor of cardiovascular events



Electrocardiographic Age Predicts Cardiovascular Events in Community: The Framingham Heart Study

Luisa C C Brant, Antônio H Ribeiro, Marcelo M Pinto-Filho, et. al.

Circulation: Cardiovascular Quality and Outcomes (2023)

Challenges

- **Interpretability** Attempt to draw real electrocardiographic **knowledge**.

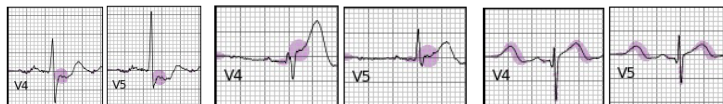


Figure: Grad-CAM plots. **(Left)** STEMI. **(Middle)** STEMI. **(Right)** NSTEMI.

Development and validation of deep learning ECG-based prediction of myocardial infarction in emergency department patients.
S. Gustafsson, D. Gedon, E. Lampa, **Antônio H. Ribeiro**, M. J. Holzmann, T. B. Schön, J. Sundström.
Scientific Reports (2022)

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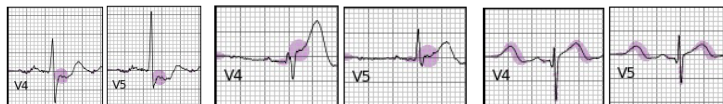


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Scientific Reports (2022)

- **Robustness.** Ability to work in **real situations**.

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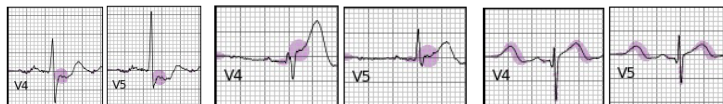


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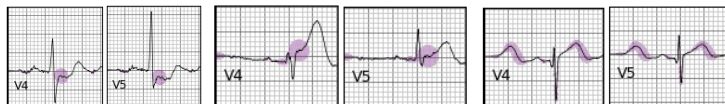


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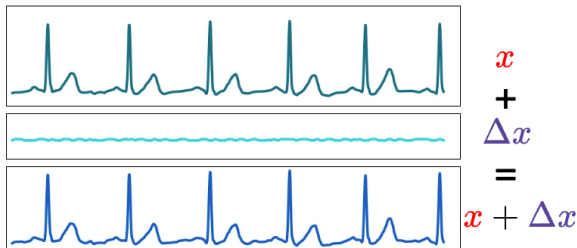
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*ML algorithms don't need to be really interpretable to be useful in clinical practice.
But they need to be robust!*

Adversarial attacks in ECGs

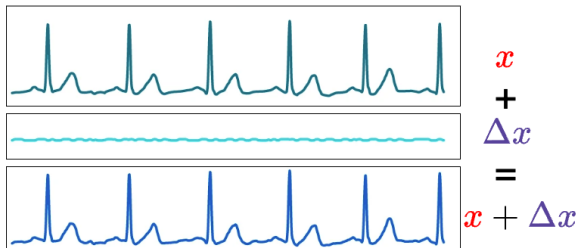
► $x \rightarrow \hat{y}$:
Normal (Probability = 0.99)



Han, X., Hu, Y., Foschini, L. et al. Deep learning models for electrocardiograms are susceptible to adversarial attacks. Nature Medicine. (2020)

Adversarial attacks in ECGs

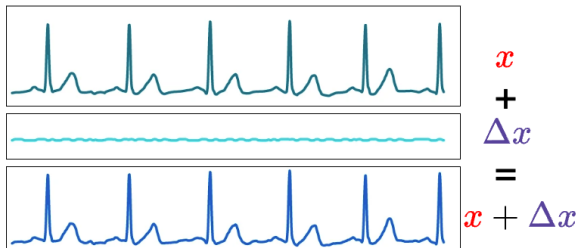
- ▶ $x \rightarrow \hat{y}$:
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- ▶ $\|\Delta x\| < \delta$



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Adversarial attacks in ECGs

- ▶ $x \rightarrow \hat{y}$:
Normal (Probability = 0.99)
- ▶ $\|\Delta x\| < \delta$
- ▶ $x + \Delta x \rightarrow \tilde{y}$:
AFib (Probability = 1.00)



Han, X., Hu, Y., Foschini, L. et al. Deep learning models for electrocardiograms are susceptible to adversarial attacks. Nature Medicine. (2020)

Conclusion

- ▶ **Large-scale models** have great potential for medicine (and critical applications).
- ▶ **Robustness** is a major challenge.
- ▶ **Adversarial attacks** framework allows for analysis of **worst-case scenarios**.
- ▶ **Linear models** for insight and analysis.
- ▶ **Adversarially-trained linear regression** is a competitive regression method.

Thank you!

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